



**UNSW SCIENCE**  
**School of Maths and Statistics**

**Course outline**

**MATH3570**  
**Foundations of Calculus**

**Term 1, 2020**



## Course Description/Aims

This course aims to re-examine the key ideas behind the Calculus and to give a deeper understanding of the notions of limit, continuity, differentiability and integrability. We will look at not only what is true, but also what is not true, in order to better understand why definitions are the way that they are, and why the conditions on the main theorems need to be there.

What does it mean for a limit to exist? What does it mean for a function to be continuous or differentiable? There are functions which are continuous everywhere but differentiable nowhere! Are there functions whose integral does not exist? In this course, we look again at the essential concepts of limit, continuity, differentiability and integrability and try to place them on a sure footing. The syllabus includes material on sequences and series of real numbers and also of real valued functions. Although of general interest to those studying mathematics for its own sake, this course is of special relevance to those planning a career in secondary teaching. MATH3570 is a compulsory component of the program for mathematics teachers.

## Assessment and Deadlines

Assessment	Week	Weighting
Pre-test	Pre-test: week 1 (in class) and end of week 9.	10
Assignment	Assignment: end of week 4.	20
Class Test	Test: week 7 (in class).	20
Final exam	Exam.	50
Total		100

## Additional Assessment Information

## Course Schedule

The course will include material taken from some of the following topics. This is should only serve as a guide as it is not an extensive list of the material to be covered and the timings are approximate. The course content is ultimately defined by the material covered in lectures.

Weeks	Topic	Reading (if applicable)
1	Introduction. Some history. What are the main theorems? How are they related? What isn't true?	Lecture notes
2	Notation: writing things clearly! Quantified statements.	Lecture notes

3	Writing analytic proofs. Limits of sequences. What are the real numbers? Supremum and infimum. Binary exp	Lecture notes
4	Sequence Monotone Convergence Theorem. Cauchy sequences.	Lecture notes
5	Limits of functions at a point. Continuity. Sequential continuity. Intermediate Value Theorem.	Lecture notes
6	Optional practice class	Lecture notes
7	Max-Min Theorem. Differentiability	Lecture notes
8	The differentiation rules. Rolle's Theorem. Mean Value Theorem.	Lecture notes
9	Integration.	Lecture notes
10	The Fundamental Theorems of Calculus.	Lecture notes
11*		Lecture notes

**\*Week 11 only applies to courses that have classes that fall on a Public Holiday**

## Textbooks

There is no set text for this course.

The content of the course will be defined by the lectures. Any book on elementary calculus (such as the standard first and second year text *Calculus: One and Several Variables* by Salas, Hille and Etgen) may prove useful. (This course is concerned only with one variable calculus).

For books more closely connected to the themes of this course, you may consult any of:

- *Calculus* by Michael Spivak (1st ed., Addison-Wesley/Benjamin, 1967; 2nd ed. Publish or Perish, 1980; 3rd ed. Cambridge Univ. Press, 2006)
- *Elementary Mathematical Analysis* by Colin Clark (2nd ed. Belmont, 1982), previously published as *The Theoretical Side of Calculus*.
- *Introduction to Analysis* by Edward D Gaughan, (5th ed., Brooks and Cole, 1998)
- *Principles of Mathematical Analysis* by Walter Rudin, (McGraw Hill, 3rd ed, 1976).
- *Real Analysis* by Frank Morgan, (1st ed. American Mathematical Society, 2005).

The book by Spivak is a classic first university level calculus text with a chatty, readable style but is also quite rigorous on proofs and the foundations of calculus. The book by Gaughan covers most of the material of this course and is closest to the aims of this course. The book by Rudin is a rather more advanced. You will not have to buy any of these books but I would highly recommend Spivak's book, if not for now, then for your future career as a mathematics teacher.

## Course Learning Outcomes (CLO)

- Demonstrate the level of understanding required to teach calculus to the next generation of mathematics students.
- Demonstrate understanding of the real number system.
- Demonstrate understanding of the formal structure of differential and integral calculus.

## Moodle

Log in to Moodle to find announcements, general information, notes, lecture slide, classroom tutorial and assessments etc.

<https://moodle.telt.unsw.edu.au>

## Computing lab

The main computing laboratory is Room G012 of the Red Centre. You can get to this lab by entering the building through the main entrance to the School of Mathematics (on the Mezzanine Level) and then going down the stairs to the Ground Level. A second smaller lab is Room M020, on the mezzanine level of the Red Centre.

For more information, including opening hours, see the computing facilities webpage:

<https://www.maths.unsw.edu.au/currentstudents/computing-facilities>

Remember that there will always be unscheduled periods when the computers are not working because of equipment problems and that this is not a valid excuse for not completing tests on time.

## School and UNSW Policies

The School of Mathematics and Statistics has adopted a number of policies relating to enrolment, attendance, assessment, plagiarism, cheating, special consideration etc. These are in addition to the Policies of The University of New South Wales. Individual courses may also adopt other policies in addition to or replacing some of the School ones. These will be clearly notified in the Course Initial Handout and on the Course Home Pages on the Maths Stats web site.

Students in courses run by the School of Mathematics and Statistics should be aware of the School and Course policies by reading the appropriate pages on the Maths Stats web site starting at:

<https://www.maths.unsw.edu.au/currentstudents/assessment-policies>

The School of Mathematics and Statistics will assume that all its students have read and understood the School policies on the above pages and any individual course policies on the

Course Initial Handout and Course Home Page. Lack of knowledge about a policy will not be an excuse for failing to follow the procedure in it.

## Academic Integrity and Plagiarism

UNSW has an ongoing commitment to fostering a culture of learning informed by academic integrity. All UNSW staff and students have a responsibility to adhere to this principle of academic integrity. Plagiarism undermines academic integrity and is not tolerated at UNSW. *Plagiarism at UNSW is defined as using the words or ideas of others and passing them off as your own.*

The **UNSW Student Code** provides a framework for the standard of conduct expected of UNSW students with respect to their academic integrity and behaviour. It outlines the primary obligations of students and directs staff and students to the Code and related procedures.

In addition, it is important that students understand that it is not permissible to buy essay/writing services from third parties as the use of such services constitutes plagiarism because it involves using the words or ideas of others and passing them off as your own. Nor is it permissible to sell copies of lecture or tutorial notes as students do not own the rights to this intellectual property.

If a student breaches the Student Code with respect to academic integrity, the University may take disciplinary action under the **Student Misconduct Procedure**.

The UNSW Student Code and the Student Misconduct Procedure can be found at:

<https://student.unsw.edu.au/plagiarism>

An online Module “[Working with Academic Integrity](https://student.unsw.edu.au/aim)” (<https://student.unsw.edu.au/aim>) is a six-lesson interactive self-paced Moodle module exploring and explaining all of these terms and placing them into your learning context. It will be the best one-hour investment you’ve ever made.

## Plagiarism

Plagiarism is presenting another person's work or ideas as your own. Plagiarism is a serious breach of ethics at UNSW and is not taken lightly. So how do you avoid it? A one-minute video for an overview of how you can avoid plagiarism can be found <https://student.unsw.edu.au/plagiarism>.

## Additional Support

### ELISE (Enabling Library and Information Skills for Everyone)

ELISE is designed to introduce new students to studying at UNSW.

Completing the ELISE tutorial and quiz will enable you to:

- analyse topics, plan responses and organise research for academic writing and other assessment tasks
- effectively and efficiently find appropriate information sources and evaluate relevance to your needs
- use and manage information effectively to accomplish a specific purpose
- better manage your time
- understand your rights and responsibilities as a student at UNSW
- be aware of plagiarism, copyright, UNSW Student Code of Conduct and Acceptable Use of UNSW ICT Resources Policy
- be aware of the standards of behaviour expected of everyone in the UNSW community
- locate services and information about UNSW and UNSW Library

Some of these areas will be familiar to you, others will be new. Gaining a solid understanding of all the related aspects of ELISE will help you make the most of your studies at UNSW.

The *ELISE* training webpages:

<https://subjectguides.library.unsw.edu.au/elise/aboutelise>

## **Equitable Learning Services (ELS)**

If you suffer from a chronic or ongoing illness that has, or is likely to, put you at a serious disadvantage, then you should contact the Equitable Learning Services (previously known as SEADU) who provide confidential support and advice.

They assist students:

- living with disabilities
- with long- or short-term health concerns and/or mental health issues
- who are primary carers
- from low SES backgrounds
- of diverse genders, sexes and sexualities
- from refugee and refugee-like backgrounds
- from rural and remote backgrounds
- who are the first in their family to undertake a bachelor-level degree.

Their web site is: <https://student.unsw.edu.au/els/services>

Equitable Learning Services (ELS) may determine that your condition requires special arrangements for assessment tasks. Once the School has been notified of these, we will make every effort to meet the arrangements specified by ELS.

Additionally, if you have suffered significant misadventure that affects your ability to complete the course, please contact your Lecturer-in-charge in the first instance.

## Academic Skills Support and the Learning Centre

The Learning Centre offers academic support programs to all students at UNSW Australia. We assist students to develop approaches to learning that will enable them to succeed in their academic study. For further information on these programs please go to:

<http://www.lc.unsw.edu.au/services-programs>

## Applications for Special Consideration for Missed Assessment

Please adhere to the Special Consideration Policy and Procedures provided on the web page below when applying for special consideration.

<https://student.unsw.edu.au/special-consideration>

Please note that the application is not considered by the Course Authority, it is considered by a centralised team of staff at the Nucleus Student Hub.

The School will contact you (via student email account) after special consideration has been granted to reschedule your missed assessment, for a *lab test or paper-based test* only.

For applications for special consideration for *assignment extensions*, please note that the new submission date and/or outcome will be communicated through the special consideration web site only, no communication will be received from the School.

For Dates on Final Term Exams and Supplementary Exams please check the “Key Dates for Exams” ahead of time to avoid booking holidays or work obligations.

<https://student.unsw.edu.au/exam-dates>

If you believe your application for Special Consideration has not been processed, you should email [specialconsideration@unsw.edu.au](mailto:specialconsideration@unsw.edu.au) immediately for advice.

## Course Evaluation and Development (MyExperience)

Student feedback is very important to continual course improvement. This is demonstrated within the School of Mathematics and Statistics by the implementation of the UNSW online student survey *myExperience*, which allows students to evaluate their learning experiences in an anonymous way. *myExperience* survey reports are produced for each survey. They are released to staff after all student assessment results are finalised and released to students. Course convenor will use the feedback to make ongoing improvements to the course.